



# Multiple View Geometry: Solution Exercise Sheet 4

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<http://vision.in.tum.de/teaching/ss2016/mvg2016>

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## Part I: Theory

### Image Formation

1. Let  $\mathbf{p} = (x \ y \ z)$  be a point on the smaller object and  $\mathbf{p}' = (x' \ y' \ z')$  a point on the larger object. Since  $\mathbf{p}'$  is twice as far away, we have  $z' = 2z$ , and twice as big we have  $x' = 2x$  and  $y' = 2y$ . Hence, it follows that  $\mathbf{p}$  and  $\mathbf{p}'$  lie on the same projection ray.

$$\pi(\mathbf{p}') = \pi \begin{pmatrix} 2x \\ 2y \\ 2z \end{pmatrix} = \begin{pmatrix} 2x/2z \\ 2y/2z \end{pmatrix} = \begin{pmatrix} x/z \\ y/z \end{pmatrix} = \pi \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \pi(\mathbf{p})$$

2. Let  $\mathbf{p}_h := \begin{pmatrix} \mathbf{p}_h \\ 1 \end{pmatrix} = (0 \ 0 \ 4 \ 1)^\top$ . Hence:

$$\tilde{\mathbf{p}}_1 = \pi(\mathbf{P}_1 \cdot \mathbf{p}_h) = \pi(-3 \ 0 \ 4)^\top = (-0.75 \ 0)^\top$$

$$\tilde{\mathbf{p}}_2 = \pi(\mathbf{P}_2 \cdot \mathbf{p}_h) = \pi(1 \ 0 \ 4)^\top = (0.25 \ 0)^\top$$

### Radial Distortion

1. No, as it can only model points for which the viewing ray intersects the image plane.
2.  $f(r) = 1 + a_1 r^2 + a_2 r^4$  is much easier to invert than  $f(r) = 1 + a_1 r + a_2 r^2 + a_3 r^3 + a_4 r^4$ . An inverse model is *needed to get 3D points* from image points and depth. (Inverting  $f$  is required for calculating the viewing ray corresponding to an image point (un-projection), this is an important property for some algorithms, like tracking algorithms.)