# A system for marker-less human motion estimation 

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#### Abstract

In this contribution we present a silhouette based human motion estimation system. The system components contain silhouette extraction based on level sets, a correspondence module, which relates image data to model data and a pose estimation module. Experiments are done in a four camera setup and we estimate the model components with 21 degrees of freedom in two frames per second. Finally, we perform a comparison of the motion estimation system with a marker based tracking system to perform a quantitative error analysis. The results show the applicability of the system for marker-less sports movement analysis.


## 1 Introduction

Human motion estimation from image sequences means to determine the rigid body motion [11] and joint angles of a 3D human model from 2D image data. Due to redundancies multi-view approaches are necessary. Often simplified models are used, e.g. by using stick, ellipsoidal, cylindrical or skeleton models [1,9,7]. We recently introduced an approach for silhouette based human motion estimation [14] which uses free-formsurface patches to estimate the pose and joint angles of the upper torso. In [15] we further applied local and global morphing techniques to get realistic motions of the upper torso model. These basic modules are now extended to a complete human motion estimation system. The system consists of an advanced image segmentation method, dynamic occlusion handling and kinematic chains of higher complexity ( 21 degrees of freedom). Finally we perform a comparison of the system with a commercial marker based tracking system [10] used to analyze sports movements ${ }^{1}$. We perform and analyze exercises, such as push ups or sit ups. The algorithm proves as stable, robust and fairly accurate.

The contribution is organized as follows: We will start with the basic setup of the motion capture system. Then we will continue with the system modules. Here we will briefly describe image segmentation based on level sets, pose estimation and the dynamic occlusion handling to deal with partial occlusion in certain frames. The next section presents the experimental results and the quantitative error analysis followed by a brief discussion.

[^0]
## 2 The human motion tracking system

A 3D object model builds the a priori knowledge of the system, which is in this case given as two free-form surface patches with two kinematic chains. Each kinematic chain


Fig. 1. The capture system consists of iterating the following steps: Segmentation, correspondence estimation, pose estimation.
consists of seven joints (three for the shoulder, two for the elbow and two for the wrist). Furthermore we added one back segment joint to the torso surface patch. The estimation procedure is dealing with 21 unknowns, six for the pose parameters (three for rotation and three for translation), 7 for each arm and one backbone joint. During correspondence estimation (along four frames) we collect around 5000 point correspondences (slightly varying dependent on the visible information) and still track in two frames per second for the four camera sequence. Using the 3D model and four images from a (triggered) calibrated camera sequence, the motion tracking system consists of three main components, namely silhouette extraction, matching and pose estimation. All components are iterated to stabilize segmentation on the one hand and pose estimation on the other hand.

### 2.1 Image segmentation

Image segmentation usually means to estimate boundaries of objects in an image. This task can become very difficult, since noise, shading, occlusion or texture information


Fig. 2. Silhouette extraction based on level set functions. Left: Initial segmentation. Right: Segmentation result.
between the object and the background may distort the segmentation or even make it impossible. Our approach is based on image segmentation based on level sets [12, 4, 5, 2]. A level set function $\Phi \in \Omega \mapsto \mathbb{R}$ splits the image domain $\Omega$ into two regions $\Omega_{1}$ and $\Omega_{2}$ with $\Phi(x)>0$ if $x \in \Omega_{1}$ and $\Phi(x)<0$ if $x \in \Omega_{2}$. The zero-level line thus marks the boundary between both regions. The segmentation should maximize the total a-posteriori probability given the probability densities $p_{1}$ and $p_{2}$ of $\Omega_{1}$ and $\Omega_{2}$, i.e., pixels are assigned to the most probable region according to the Bayes rule. Ideally, the boundary between both regions should be as small as possible. This can be expressed by the following energy functional that is sought to be minimized:

$$
\begin{equation*}
E\left(\Phi, p_{1}, p_{2}\right)=-\int_{\Omega}\left(H(\Phi) \log p_{1}+(1-H(\Phi)) \log p_{2}+\nu|\nabla H(\Phi)|\right) d x \tag{1}
\end{equation*}
$$

where $\nu>0$ is a weighting parameter and $H(s)$ is a regularized version of the Heaviside function, e.g. the error function. Minimization with respect to the region boundary represented by $\Phi$ can be performed according to the gradient descent equation

$$
\begin{equation*}
\partial_{t} \Phi=H^{\prime}(\Phi)\left(\log \frac{p_{1}}{p_{2}}+\nu \operatorname{div}\left(\frac{\nabla \Phi}{|\nabla \Phi|}\right)\right) \tag{2}
\end{equation*}
$$

where $H^{\prime}(s)$ is the derivative of $H(s)$ with respect to its argument. The probability densities $p_{i}$ are estimated according to the expectation-maximization principle. Having the level set function initialized with some contour, the probability densities within the two regions are estimated by the gray value histograms smoothed with a Gaussian kernel $K_{\sigma}$ and its standard deviation $\sigma$.

This rather simple and fast approach is sufficient for our laboratory set-up, though it is also conceivable to apply more elaborated region models including texture features. Figure 2 shows an example image and the contour evolution over time. As can be seen, the body silhouette is well extracted, but there are some deviations in the head region, due to the dark hair. Such inaccuracies can be compensated from the pose estimation procedure. For our algorithm we can make a tracking assumption. Therefore, we initialize the silhouette with the pose of the last frame which greatly reduces the number of iterations needed. The implementation is fast; the algorithm needs 50 ms per frame and 200 ms image processing time for a four-camera setup.

### 2.2 Pose estimation

For pose estimation we assume a set of point correspondences $\left(X_{i}, x_{i}\right)$, with 4D (homogeneous) model points $X_{i}$ and 3D (homogeneous) image points $x_{i}$. Each image point is reconstructed to a Plücker line $L_{i}=\left(n_{i}, m_{i}\right)$, with a (unit) direction $n_{i}$ and moment $m_{i}$ [11].

Every 3D rigid motion can be represented in an exponential form

$$
M=\exp (\theta \hat{\xi})=\exp \left(\begin{array}{cc}
\hat{\omega} & \boldsymbol{v} \\
0_{3 \times 1} & 0
\end{array}\right)
$$

where $\theta \hat{\xi}$ is the matrix representation of a twist $\xi=\left(\omega_{1}, \omega_{2}, \omega_{3}, v_{1}, v_{2}, v_{3}\right) \in \operatorname{se}(3)=$ $\left\{(\boldsymbol{v}, \omega) \mid \boldsymbol{v} \in \mathbf{R}^{3}, \omega \in \operatorname{so}(3)\right\}$, with $s o(3)=\left\{\boldsymbol{A} \in \mathbf{R}^{3 \times 3} \mid \boldsymbol{A}=-\boldsymbol{A}^{T}\right\}$.

In fact, $\boldsymbol{M}$ is an element of the one-parametric Lie group $S E(3)$, known as the group of direct affine isometries. A main result of Lie theory is, that to each Lie group there exists a Lie algebra which can be found in its tangential space, by derivation and evaluation at its origin; see [11] for more details. The corresponding Lie algebra to $S E(3)$ is denoted as $s e(3)$. A twist contains six parameters and can be scaled to $\theta \xi$ with a unit vector $\omega$. The parameter $\theta \in \mathbb{R}$ corresponds to the motion velocity (i.e., the rotation velocity and pitch). For varying $\theta$, the motion can be identified as screw motion around an axis in space. To reconstruct a group action $\boldsymbol{M} \in S E(3)$ from a given twist, the exponential function $\exp (\theta \hat{\xi})=\boldsymbol{M} \in S E(3)$ must be computed. This can be done efficiently by using the Rodriguez formula [11],

$$
\exp (\hat{\xi} \theta)=\left(\begin{array}{cc}
\exp (\theta \hat{\omega}) & (I-\exp (\hat{\omega} \theta))(\omega \times \boldsymbol{v})+\omega \omega^{T} \boldsymbol{v} \theta \\
0_{1 \times 3} & 1
\end{array}\right), \text { for } \omega \neq 0
$$

with $\exp (\theta \hat{\omega})$ computed by calculating

$$
\exp (\theta \hat{\omega})=I+\hat{\omega} \sin (\theta)+\hat{\omega}^{2}(1-\cos (\theta)) .
$$

Note that only sine and cosine functions of real numbers need to be computed.
For pose estimation we combine the reconstructed Plücker lines with the screw representation for rigid motions and apply a gradient descent method: Incidence of the transformed 3D point $X_{i}$ with the 3D ray $L_{i}$ can be expressed as

$$
\left(\exp (\theta \hat{\xi}) X_{i}\right)_{3 \times 1} \times n_{i}-m_{i}=0
$$

Indeed, $X_{i}$ is a homogeneous 4D vector, and after multiplication with the $4 \times 4$ matrix $\exp (\theta \hat{\xi})$ we neglect the homogeneous component (which is 1 ) to evaluate the cross product with $n_{i}$. We now linearize the equation by using $\exp (\theta \hat{\xi})=\sum_{k=0}^{\infty} \frac{(\theta \hat{\xi})^{k}}{k!} \approx$ $\boldsymbol{I}+\theta \hat{\xi}$, with $\boldsymbol{I}$ as identity matrix. This results in

$$
\left((\boldsymbol{I}+\theta \hat{\xi}) X_{i}\right)_{3 \times 1} \times n_{i}-m_{i}=0
$$

and can be reordered into an equation of the form $\boldsymbol{A} \xi=\boldsymbol{b}$. Collecting a set of such equations (each is of rank two) leads to an overdetermined system of equations, which can be solved using, for example, the Householder algorithm. The Rodriguez formula can be applied to reconstruct the group action $\boldsymbol{M}$ from the estimated twist $\xi$. Then
the 3 D points can be transformed and the process is iterated until the gradient descent approach converges.

Joints are expressed as special screws with no pitch of the form $\theta_{j} \hat{\xi_{j}}$ with known $\hat{\xi}_{j}$ (the location of the rotation axes as part of the model representation) and unknown joint angle $\theta_{j}$. The constraint equation of a $j$ th joint has the form

$$
\left(\exp \left(\theta_{j} \hat{\xi_{j}}\right) \ldots \exp \left(\theta_{1} \hat{\xi_{1}}\right) \exp (\theta \hat{\xi}) X_{i}\right)_{3 \times 1} \times n_{i}-m_{i}=0
$$

which is linearized in the same way as the rigid body motion itself. It leads to three linear equations with the six unknown pose parameters and $j$ unknown joint angles. Collecting a sufficient number of equations leads to an overdetermined system of equations.

Note, that since we work with reconstructed 3D lines, we can gain equations from different cameras (calibrated with respect to the same world coordinate system) and put them together in one system of equations and solve them simultaneously. This is the key idea to deal with partial occlusions: A joint which is not visible in one camera must be visible in another one to get a solvable system of equations. A set of four cameras around the subject covers a large range and allows to analyze quite complex motion patterns.

### 2.3 Correspondence estimation

After image segmentation correspondences between the object model and the extracted silhouettes are established. Therefore, we follow a modified version of an ICP algorithm [14] and use a voting method to decide, whether a point belongs to the torso or one of the arms. These correspondences are applied on the pose estimation module resulting in a slightly transformed object. This is used to establish new correspondences until the overall pose converges.

## 3 Experiments

A lack of many studies is that only a visual feedback about the pose result is given, by overlaying the pose result with the image data, e.g. [14]. To enable a quantitative error analysis, we use a commercial marker based tracking system for a comparison. Here, we use the Motion Analysis software [10], with an 8-Falcon-camera system. For data capture we use the Eva 3.2.1 software and the Motion Analysis Solver Interface 2.0 for inverse kinematics computing [10]. In this system a human has to wear a body suit and retroflective markers are attached to it. Around each camera is a strobe light led ring and a red-filter is in front of each lens. This gives very strong image signals of the markers in each camera. These are treated as point markers which are reconstructed in the eight-camera system. The system is calibrated by using a wand-calibration method. Due to the filter in front of the images we had to use a second camera set-up which provides real image data. This camera system is calibrated by using a calibration cube. After calibration, both camera systems are calibrated with respect to each other. Then


Fig. 3. The coordinate systems in the lab setup.


Fig. 4. Tracked arms: The angle diagrams show the elbow values of the Motion analysis system (dotted) and the silhouette system (solid).


Fig. 5. Tracked Push-ups: The angle diagrams show the elbow values of the Motion analysis system (dotted) and the silhouette system (solid).
we generate a stick-model from the point markers including joint centers and orientations. This results in a complete calibrated set-up we use for a system comparison. It is visualized in figure 3.

The images in the upper left of figure 1 show the body-suit with the attached markers. These lead to minor errors during silhouette extraction, which are omitted here. Figure 4 shows the first test sequence, where the subject is just moving the arms forwards and backwards. The diagram on the right side shows the estimated angles of the right elbow. The marker results are given as dotted lines and the silhouette results in solid lines. The overall error between both angles diagrams is 2.3 degrees, including the tracking failure between frames 200 till 250 .

Figure 5 shows the second test sequence, where the subject is performing a series of push-ups. Here the elbow angles are much more characteristic and also well comparable. The overall error is 1.7 degrees. Both sequences contain partial occlusions in certain frames. But this can be handled from the algorithm.

## 4 Discussion

The contribution presents a human motion estimation system. The system extracts silhouettes by using level-set functions and uses a model with 21 degrees of freedom in a four-camera set-up. Finally we perform a comparison of the marker-free approach with a commercial marker based tracking system. In [13] eight bio-mechanical measurement systems are compared (including the Motion Analysis system). There is also performed a rotation experiment which shows, that the RMS $^{2}$ errors are typically within three degrees. Our error measures fit in this range quite well.

Marker-less human motion tracking is highly challenging for sports, exercise and clinical analysis and the system evaluation shows, that our approach is leading in the

[^1]right direction for a marker-less stable and accurate human motion estimation system. Future works will continue with silhouette extraction in more complex environments, so that we can also analyze sports movements in non-lab environments.

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[^0]:    ${ }^{1}$ Motion Analysis Corporation is one of the leading provider of optical motion capture systems in entertainment, video-games, film, broadcasting, virtual reality, medicine, sports, and research.

[^1]:    ${ }^{2}$ root mean square

